

- ROBERTSON, J. M. (1936). *Proc. Roy. Soc. A* **157**, 79.  
 ROBERTSON, J. M. & UBBELOHDE, A. R. (1938). *Proc. Roy. Soc. A* **167**, 122.  
 ROBERTSON, J. M. & UBBELOHDE, A. R. (1939). *Proc. Roy. Soc. A* **170**, 222.  
 ROBERTSON, J. M. & WOODWARD, I. (1936). *J. Chem. Soc.* p.1817.  
 ROBINSON, W. T. & IBERS, J. A. (1967). *Inorg. Chem.* **6**, 1208.  
 SABINE, T. M., COX, G. W. & CRAVEN, B. M. (1969). *Acta Cryst.* **B25**, 2437.  
 STEWART, R. F., DAVIDSON, E. R. & SIMPSON, W. T. (1965). *J. Chem. Phys.* **42**, 3175.  
 TOMITA, K., RICH, A., DE LOZE, C. & BLOUT, E. R. (1962). *J. Mol. Biol.* **4**, 83.  
 UBBELOHDE, A. R. & GALLAGHER, K. J. (1955). *Acta Cryst.* **8**, 71.  
 UBBELOHDE, A. R. & WOODWARD, I. (1942). *Proc. Roy. Soc. A* **179**, 399.  
 ZACHARIASEN, W. H. (1963). *Acta Cryst.* **16**, 1139.  
 ZACHARIASEN, W. H. (1965). *Acta Cryst.* **18**, 705.  
 ZACHARIASEN, W. H. (1968). *Acta Cryst. A* **24**, 212.

*Acta Cryst.* (1969). **B25**, 2437

## A Neutron Diffraction Study of $\alpha$ -Oxalic Acid Dihydrate

BY T. M. SABINE AND G. W. COX

Materials Division, AAEC Research Establishment, Lucas Heights, N.S.W., Australia

AND B. M. CRAVEN

Crystallography Laboratory, University of Pittsburgh, Pittsburgh, Pennsylvania 15213, U.S.A.

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A determination of the crystal structure of  $\alpha$ -oxalic acid dihydrate from three-dimensional neutron diffraction data has confirmed, with greater precision, the atomic parameters found previously from  $h0l$  and  $0kl$  data. Assumptions concerning the vibration state of the molecule are shown to introduce uncertainties in bond lengths much greater than the standard deviations derived from least-squares refinement of atomic parameters. The extent to which data collection at low temperature would reduce the uncertainty is calculated.

### Introduction

The crystal structure of  $\alpha$ -oxalic acid dihydrate (here abbreviated  $\alpha$ -POX) has been investigated several times by X-ray diffraction methods. Ahmed & Cruickshank (1953) obtained the positions of the carbon and oxygen atoms by a re-examination of earlier two-dimensional data of Robertson & Woodward (1936) and Brill, Hermann & Peters (1942). Garrett (1954) carried out a neutron diffraction investigation and located the hydrogen atoms from  $h0l$  and  $0kl$  data.

The present three-dimensional neutron structure determination has been carried out in order to obtain more precise atomic parameters (particularly for the hydrogen atoms), to examine the effects of assumptions about the atomic anisotropic thermal motions on the observed bond lengths, and to enable a more complete comparison between X-ray and neutron diffraction studies of this material ( $\alpha$ -POX, Delaplane & Ibers, 1969), and the two deuterated crystalline forms ( $\alpha$ -DOX and  $\beta$ -DOX, Coppens & Sabine, 1969).

### Experimental

The crystals of oxalic acid dihydrate were obtained from Dr A. McL. Mathieson of the Division of Chemical Physics, C.S.I.R.O., Melbourne.

The crystal data (from Delaplane & Ibers, 1969) are:

Space group  $C_{2h}^5 - P2_1/n$ ,  
 $a = 6.119$ ,  $b = 3.607$ ,  $c = 12.057 \text{ \AA}$ ,  $\beta = 106^\circ 19'$ ,  $Z = 2$ .

Two crystals were used, one of mass 36.65 mg and one of mass 2.75 mg. Most of the data were obtained from the larger crystal which was pillar shaped with well developed  $\{101\}$ ,  $\{10\bar{1}\}$  and  $\{001\}$  forms. The small crystal was cut to a rough cube.

### Data collection

The data were collected on two single-crystal diffractometers installed on the reactor HIFAR. For these instruments the respective fluxes and wave lengths of the monochromatic neutron beam at the specimen are  $2.8 \times 10^5 \text{ n cm}^{-2} \text{ sec}^{-1}$  at  $1.10 \text{ \AA}$ , and  $6 \times 10^6 \text{ n cm}^{-2} \text{ sec}^{-1}$  at  $1.09 \text{ \AA}$ .

The large crystal was mounted on a two-circle goniometer with  $\mathbf{c}^*$  along the  $\varphi$  axis so that a  $\varphi$ -rotation would present maximum and minimum path lengths for the incident and diffracted beams of  $00l$  reflections and enable extinction and absorption effects to be detected. Both effects were apparent. However, the integrated intensities  $00l$  observed at a  $\varphi$ -setting half way between the minimum and maximum neutron path length positions were 30 per cent larger than those

observed at the minimum path length position. This effect could only be attributed to an anisotropic mosaic spread\* such that in crystal sections taken parallel to the *ab* plane, there is greater rumpling of the mosaic structure along the **b** direction than along **a**. When the smaller crystal was examined with the high flux neutron beam, the same anisotropic extinction effect was present but in this case the maximum variation in integrated intensity was only 9 per cent.

The neutron intensity data collected for  $\alpha$ -POX consisted of three subsets of data, with appropriate overlap to permit these to be placed on the same relative scale. Firstly, 708 reflections were measured from the large crystal with the low flux beam; of these, 90 were rejected.

\* A similar observation was made by Delaplane & Ibers (1969) in their X-ray study of  $\alpha$ -POX.

ted because of severe extinction and 209 were not above background. Secondly, the weak reflections were remeasured from the large crystal with the high flux beam; the number of unobservably weak reflections was reduced to 119. Thirdly, the 90 reflections rejected from the first data were remeasured from the small crystal with the high flux beam. No attempt was made to correct these data for extinction effects.

For the intensity measurements the diffractometers were operated by step scanning in the  $\theta:2\theta$  mode controlled by monitor counters. The numbers of counts per step ( $3'$  of  $2\theta$ ) were punched on paper tape. The length of the scan was such that the peak occupied the central third of the  $2\theta$  range. In extracting the intensities the background was taken as close as possible to the peaks in order to make an empirical allowance for diffuse scattering at and around the Bragg position.

Table 1. Observed and calculated structure factors (f units)

Asterisks mark unobservably weak reflections. Columns are:  $l$  index,  $|F_{\text{obs}}|$ ,  $F_{\text{calc}}$ .

2	398	355	2	51	-7	16	165	170	-6	38	-6	40	31	2	52	43	-2	62	60	1	21	46	43					
4	134	123	4	268	251	-15	43	46	-5	61	68	-5	43	46	4	14*	15	-1	160	169	H	0	K	4				
6	366	312	8	92	86	-16	14*	21	-2	14	18	33*	-4	78	88	5	14*	15	-1	187	188	H	0	14*	4			
8	529	484	7	102	97	-12	10	12	-2	20	38	-3	111	106	6	51	51	1	13*	5	1	38	30*	1	127	137		
10	528	493	H	2	K	-1	12	101	112	-2	22	27	-3	224	247	6	106	105	-1	205	204	H	0	14*	4			
12	528	493	67	-11	273	266	-11	130	111	-1	176	214	-1	60	53	8	172	155	-3	45	46	3	102	107				
14	195	202	-9	30	20	-12	229	235	-1	66	77	0	276	305	H	6	K	2	4	337	346	4	33	27				
16	14*	4	-7	157	141	-1	157	143	-2	64	74	1	61	56	-12	111	109	5	178	176	5	100	99					
-1	11	10	H	2	K	-3	135	123	-8	71	57	-3	107	106	2	29	302	-11	222	207	6	97	99	6	36	37		
-3	14	10	-1	42	40	-1	131	121	-5	59	60	100	104	3	15*	17	102	7	14*	16	7	44	49					
-5	245	231	7	16	16	1	16	13	2	59	60	104	104	-2	14*	16	102	7	14*	16	1	16	15					
-7	52	45	H	8	K	-9	-5	114	91	-6	57	44	5	102	92	-8	29	31	9	143	135	9	14*	24				
-9	34	25*	-8	105	107	-3	371	350	-1	84	96	4	106	101	-7	95	84	10	153	157	10	84	83					
-11	372	405	-6	14*	22	-2	33	43	-4	H	7	K	1	7	162	151	-6	55	47	11	14*	9	H	0	K	4		
-13	441	441	-5	2	250	250	-12	151	165	-3	183	169	-5	54	59	-5	159	147	H	3	K	3	-9	131	140			
-15	217	220	-2	74	74	-1	167	167	-1	108	108	108	108	-1	193	192	-12	140	107	5	50	54	10	37	36			
-17	37	31	0	122	127	-1	196	196	-10	62	62	106	106	-1	193	192	-12	140	107	5	50	54	10	37	36			
7	422	411	H	6	K	1	1	173	178	-9	14*	14	7	11	79	79	-2	14*	14	7	11	206	204	6	177	174		
9	203	184	2	5*	4*	2	12	12	-6	81	41	35	12	91	96	-11	114	104	-10	76	76	-5	52	52				
11	187	161	3	63	59	3	67	64	-7	156	157	13	59	61	0	112	102	-9	70	65	4	128	126					
13	31	31	9	24	24	5	29	29	-1	130	130	15	15	157	157	1	204	203	2	81	30	-8	36	25	-3	56	52	
15	117	117	6	16	16	1	16	16	-2	59	54	53	53	63	63	-4	14*	14	6	157	155	2	45	45	-5	59	56	
H	2	K	U	7	225	231	6	243	275	7	13	23	-3	43	32	-13	111	106	4	81	81	-5	113	111	-1	47	47	
-16	226	262	9	262	278	7	13	23	-2	14*	14	14*	14	12	91	78	5	14*	32	-4	99	93	1	32	41			
18	111	88	18	242	256	8	215	225	-1	9	72	0	151	158	-11	138	127	6	14*	2	-3	192	191	2	14*	15		
20	291	275	11	374	320	10	55	79	-1	14*	14	5	10	46	29	H	7	K	2	13*	21	4	14*	21				
22	8	320	317	14	78	11	14*	14	-1	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14			
-24	111	100	H	1	K	1	12	57	58	-5	31	121*	45	-8	47	38	-9	34	22	0	31	25	5	102	102			
-4	424	491	-16	113	131	H	4	K	1	4	89	89	-7	269	269	5	95	77	1	125	118	2	121	124				
-2	70	74	156	236	231	-15	243	236	H	8	K	1	6	157	147	-7	34	44	2	186	182	7	40	45				
0	110	114	52	16	16	14*	22	-2	8	14*	22	-5	380	394	-6	14*	14	3	14*	14	8	14*	14					
2	182	182	4	16	16	14*	22	-3	103	103	111	-8	46	46	-3	198	198	5	57	56	7	157	156					
4	80	82	-12	57	57	-15	36	16	-4	14*	14	3	198	193	7	112	112	3	36	43	8	14*	14					
6	456	454	11	236	219	-11	14	14	-2	64	58	-6	21	69	-6	14*	14	3	14*	14	8	14*	14					
8	242	217	-10	34	329	-19	109	112	-3	48	66	-1	122	118	-2	14*	14	16	7	123	117	-7	79	83				
10	102	95	-9	19	181	8	58	64	-2	34	29	0	310	335	-1	58	58	14*	14	16	-6	96	109					
12	83	74	-7	288	288	-1	150	150	-1	12	121	1	61	68	0	65	58	9	92	85	-5	117	114					
14	43	53	7	210	210	-2	282	297	-1	62	64	3	265	265	2	39	39	-12	180	174	H	0	K	109				
H	3	K	0	-7	77	73	-6	162	164	-3	140	141	3	265	265	2	39	39	-12	180	174	H	0	K	109			
-15	419	433	-5	214	211	-5	253	275	-1	93	101	4	282	295	H	0	K	3	-11	123	-9	114	123					
-13	25	25	-20	23	23	-5	55	59	2	54	63	5	281	291	1	65	63	10	192	182	H	0	11	139				
-11	134	132	-3	272	219	-2	212	229	-2	228	229	2	66	63	2	186	189	-9	35	32	1	70	61					
-9	347	347	1	16	16	14*	22	-2	44	44	5	131	144	7	112	112	3	36	43	11	16	110						
-7	27	29	-1	195	195	-1	158	160	-1	158	160	16	16	16	-2	208	208	-7	42	42	5	104	106					
-5	379	395	-1	243	243	-1	156	176	-7	317	317	314	-9	107	98	5	32	28	4	34	34	17*	17					
-3	294	286	1	127	129	1	102	111	9	64	81	10	99	110	6	87	82	1	179	172	5	139	136					
1	12*	18	2	162	145	2	171	177	-10	126	119	11	14*	14	7	12	7	36	36	-4	39	34	6	14*	14			
3	224	207	3	256	256	3	368	323	11	13*	13*	13	13*	13*	3	104	104	8	141	140	-3	14*	12	7	85	91		
5	5	5	13	13	13	13	259	259	13	13	13	13	13	13	-13	94	84	17	14*	14	22	-2	105	118	H	0	K	4
7	75	76	5	39	32	5	135	133	13	13	13	13	13	13	-13	94	84	17	14*	14	22	-2	105	118	H	0	K	4
9	308	297	6	299	285	6	71	51	14	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14			
11	14*	14*	7	297	278	7	41	55	H	1	K	2	-1	232	211	-12	64	56	54	171	164	1	79	70	-7	47	47	
13	14*	14*	9	225	234	8	121	128	-15	15	15	15	15	15	15	15	15	15	15	15	15	15	15	15				
H	4	K	0	-9	15*	15*	15	15	15	15	15	15	15	15	15	15	15	15	15	15	15	15	15	15	15			
-16	76	84	10	245	257	17*	15	15	-2	220	226	4	171	161	-1	44	44	5	35	35	1	76	74	4	76	82		
-12	80	77	11	18*	16*	1	11	11	71	68	-7	122	116	-11	26	26	5	55	55	55	55	55	55	55				
-12	107	104	12	14	14	-15	42	50	-13	33	34	-6	268	254	-10	81	77	6	92	91	-2	91	105					
-10	173	157	13*	98	100	-14	26	-2	-16	131	136	-4	299	291	-8	55	63	8	130	119	3	158	166					
-8	95	87	14	99	96	-16	140	-2	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14				
-6	247	273	H	2	K	-1	125	125	135	135	135	135	135	135	135	135	135	135	135	135	135	135	135	135				
-2	534	510	-16	14*	22	-2	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14				
-9	209	195	11*	15	151	298	-9	36	38	-1	268	293	9	96	96	-4	50	49	-9	75	77	4	44	46				
-2	69	62	-12	141	145	-8	14*	15	-3	164	167	1	31	31	-3	35	39	-8	14*	3	14*	3	5	14*	3			
-4	262	266	14	14*	14	34	-7	74	74	-2	116	111	-11	82	82	-8	123	126	-7	36	31	6	14*	9				
-6	230	252	11*	151	151	24	24	24	-1	150	148	14*	14	14*	14	14*	14	14*	14	14*	14	14*	14					
-2	72	254	-11	317	310	-5	74	70	-2																			

### Analysis of data

#### 1. Absorption correction

Absorption effects in hydrogen-containing crystals are due to the high incoherent scattering cross-section of hydrogen. In making a correction there is an uncertainty about the appropriate value of this cross section. The free atom cross-section for hydrogen is 20 barns while application of the usual relationship between free and bound cross sections predicts  $\sigma_{\text{bound}}$  to be 80 barns. For neutrons of the wavelength used in these experiments the cross section lies between these values since

an indeterminate but appreciable energy interchange takes place. The appropriate incoherent cross-section was chosen to be that of hydrogen in water which was measured as 34 barns at the neutron energies used in this work. This value agrees with that of Melkonian (1949). The observed intensities were corrected by numerical integration over the neutron path length in the crystal.

#### 2. Weighting the data

It was realized that basing the weight on the statistical errors alone would give an unrealistically high

Table 2. Fractional positional and thermal parameters of all atoms with their standard deviations

Thermal parameters are in the form  $\exp[-(\beta_{11}h^2 + \beta_{22}k^2 + \beta_{33}l^2 + 2\beta_{12}hk + 2\beta_{13}hl + 2\beta_{23}kl)]$ . All parameters and e.s.d.'s are expressed  $\times 10^4$ .

	$x, \sigma(x)$	$y, \sigma(y)$	$z, \sigma(z)$	$\beta_{11}, \sigma(\beta_{11})$	$\beta_{22}, \sigma(\beta_{22})$	$\beta_{33}, \sigma(\beta_{33})$	$\beta_{12}, \sigma(\beta_{12})$	$\beta_{13}, \sigma(\beta_{13})$	$\beta_{23}, \sigma(\beta_{23})$
C(1)	-452 (2)	547 (4)	510 (1)	169 (4)	462 (11)	27 (1)	49 (4)	21 (1)	1 (2)
O(1)	847 (4)	-599 (6)	1488 (2)	228 (6)	827 (18)	29 (1)	143 (7)	19 (2)	7 (3)
O(2)	-2197 (3)	2310 (6)	360 (2)	224 (6)	838 (17)	32 (1)	184 (7)	26 (2)	7 (3)
O(3)	-4509 (4)	6136 (6)	1799 (2)	219 (6)	829 (17)	33 (1)	69 (8)	31 (2)	22 (3)
H(1)	293 (7)	93 (12)	2189 (3)	285 (10)	945 (29)	45 (2)	58 (14)	32 (4)	4 (6)
H(2)	-5740 (7)	6864 (13)	1142 (3)	314 (12)	1083 (35)	50 (3)	105 (17)	24 (4)	47 (7)
H(3)	-3599 (9)	4447 (14)	1508 (4)	343 (13)	1097 (40)	79 (3)	126 (19)	66 (5)	15 (9)

Table 3. Bond lengths for  $\alpha$ -POX and  $\alpha$ -DOX

The e.s.d.'s given in brackets refer to the least significant digits in the bond lengths.

	$\alpha$ -POX This investigation (neutron)	$\alpha$ -POX Ahmed & Cruickshank (X-ray)	$\alpha$ -POX Garrett (neutron)	$\alpha$ -POX Delaplane & Ibers (X-ray)	$\alpha$ -DOX Coppens & Sabine (neutron)
C(1)-C(1)	1.536 (3) Å	1.529 (20) Å	1.533 (11) Å	1.538 (2) Å	1.539 (2) Å
C(1)-O(1)	1.291 (5)	1.285 (12)	1.254 (8)	1.285 (1)	1.291 (2)
C(1)-O(2)	1.212 (4)	1.187 (22)	1.229 (14)	1.212 (1)	1.208 (2)
O(1)-H(1)	1.026 (7)		1.057 (16)		1.031 (2)
O(3)-H(2)	0.964 (7)		0.968 (29)		0.954 (2)
O(3)-H(3)	0.956 (9)		0.945 (21)		0.954 (2)
H(1)···O(3 <sup>iii</sup> )	1.480 (7)				1.493 (2)
H(2)···O(2 <sup>iii</sup> )	1.917 (8)				1.939 (2)
H(3)···O(2 <sup>iv</sup> )	1.979 (9)				2.008 (2)
O(1)···O(3 <sup>ii</sup> )	2.506 (4)	2.491 (8)	2.518 (8)	2.512 (1)	2.524 (2)
O(3)···O(2 <sup>iii</sup> )	2.864 (5)	2.879 (9)		2.864 (2)	2.879 (2)
O(3)···O(2 <sup>iv</sup> )	2.881 (4)	2.885 (18)		2.883 (1)	2.906 (2)

Table 4. Bond angles for  $\alpha$ -POX and  $\alpha$ -DOX

The e.s.d.'s given in brackets refer to the least significant digits in the bond angles.

	$\alpha$ -POX This investigation (neutron)	$\alpha$ -POX Ahmed & Cruickshank (X-ray)	$\alpha$ -POX Garrett (neutron)	$\alpha$ -POX Delaplane & Ibers (X-ray)	$\alpha$ -DOX Coppens & Sabine (neutron)
O(1)-C(1)-O(2)	126.6 (3)°	125.8 (14)°	126.7 (9)°	126.8 (1)°	126.6 (1)°
O(1)-C(1)-C(1 <sup>i</sup> )	112.4 (3)	112.6 (10)	112.3 (7)	112.1 (1)	112.2 (1)
O(2)-C(1)-C(1 <sup>i</sup> )	121.0 (3)	121.6 (11)	120.9 (8)	121.1 (1)	121.2 (1)
C(1)-O(1)-H(1)	114.4 (6)				112.8 (1)
H(2)-O(3)-H(3)	105.9 (7)		105.8 (17)		105.8 (2)
O(1)-H(1)···O(3)	179.3 (6)		175.3 (20)		177.4 (1)
H(1)···O(3)-H(2)	112.8 (7)		112.9 (30)		113.7 (1)
H(1)···O(3)-H(3)	116.8 (4)				116.8 (1)
O(3)-H(2)···O(2 <sup>iii</sup> )	166.9 (6)				167.7 (2)
H(2)···O(2 <sup>iii</sup> )-C(1 <sup>iii</sup> )	122.8 (6)				123.1 (1)
O(3)-H(3)···O(2 <sup>iv</sup> )	156.6 (7)		156.1 (30)		156.0 (2)
H(3)···O(2 <sup>iv</sup> )-C(1 <sup>iv</sup> )	129.5 (7)				129.6 (1)

weight to the intense reflections and so the standard deviation of an observed structure amplitude was assumed to be

$$\sigma(F) = \sigma + 0.05|F|$$

where  $\sigma$  is the estimated standard deviation based on counting statistics.

The unobservably small structure amplitudes were assigned values of  $0.4 F_{\min}$  with e.s.d.'s of  $0.2 F_{\min}$  where  $F_{\min}$  is the minimum observable value of a structure amplitude at the corresponding Bragg angle.

### 3. Structure refinement

The structure parameters were refined and interpreted using the computer programs *ORFLS* and *ORFFE* (Busing, Martin & Levy, 1962*a, b*). The initial parameters were those found by Baur (private communication) from a re-analysis of Garrett's data. The scattering lengths were set at  $O=5.8$  f,  $C=6.61$  f and  $H=-3.78$  f.\* An overall scale factor and the positional parameters and anisotropic temperature factors for each atom were varied. The refinement was based on  $F$  and each reflection was weighted according to the standard deviations found above.

The final discrepancy factors were:

- (1)  $R$  including all reflections, 0.083 ;
- (2)  $R$  omitting unobserved reflections, 0.072;
- (3) Weighted  $R$ , omitting unobserved reflections, 0.092 .

In Table 1 the calculated and observed structure factors are compared. Table 2 gives the positional and thermal parameters for each atom with their standard deviations.

### Discussion

#### 1. Bond lengths and bond angles

Bond lengths and bond angles are shown in Tables 3 and 4 together with the corresponding values found for  $\alpha$ -POX by other investigators and for  $\alpha$ -DOX by Coppens & Sabine (1969).

The present neutron results for the carbon and oxygen atom configuration in the  $\alpha$ -POX structure agree with the X-ray results within experimental error, thus helping to confirm the observations of Delaplane & Ibers (1969), that there are no significant differences in the heavier atom geometry of the oxalic acid molecule in  $\alpha$ -POX and  $\alpha$ -DOX and that the major effects of deuteration are in the significant lengthening of the  $O \dots O$  distances in all three hydrogen bonds.

A comparison of our neutron results for  $\alpha$ -POX with those of Coppens & Sabine (1969) for  $\alpha$ -DOX shows good agreement between the proton and deuteron intramolecular configurations, *e.g.* the covalent bond lengths involving hydrogen atoms and the bond angle in the water molecule are the same within experimental error. However, the bond angle  $C-O(1)-H(1)$  shows a de-

crease ( $1.6^\circ$ ) on deuteration, which is possibly significant in terms of its e.s.d. ( $0.6^\circ$ ).

It is interesting to note that isotopic substitution has no effect, within experimental error, on the angular relationships at the hydrogen atoms in the two longer hydrogen bonds. Deuteration results simply in lengthening the  $H(2) \dots O(2^{ii})$  and  $H(3) \dots O(2^{iv})$  distances by 0.022 and 0.029 Å, with e.s.d.'s of 0.009 Å in both cases. The corresponding lengthenings of  $O \dots O$  distances are 0.015 and 0.025 Å with e.s.d.'s of 0.006 and 0.005 Å respectively. In the short hydrogen bond, the isotope effect may be more complex, since, in addition to a slight but significant increase in  $O(1) \dots O(3^{ii})$  distance (0.018 Å with e.s.d. of 0.005 Å) deuteration results in a possibly significant bending ( $1.9^\circ$  with e.s.d. of  $0.6^\circ$ ) in the angle  $O(1)-H(1) \dots O(3^{ii})$ . This is associated with the decrease in  $C-O(1)-H(1)$  angle described above.

#### 2. Thermal parameters

Each bond length in  $\alpha$ -POX is subject to a correction which is uncertain, to the extent that it depends on assumptions as to the relative thermal vibrational behaviour of the atoms involved. The small differences in atomic configuration between  $\alpha$ -POX and  $\alpha$ -DOX will not be greatly affected in this way because the vibrational behaviour in the two crystal structures should be very similar. However, in Table 5, it is shown that the two sets of bond lengthenings introduced by assuming the riding and the independent modes of thermal motion (Busing, & Levy, 1964) may in some bonds differ by an order of magnitude greater than the e.s.d.'s in the uncorrected bond lengths.

Table 5. Bond lengths corrected for thermal motion

- (1) Separation of mean positions of atoms with e.s.d.
- (2) Corrected for thermal motion assuming second atom riding on first.
- (3) Corrected for thermal motion assuming independent thermal motion.

	(1)	(2)	(3)
$C(1)-C(1)$	1.536 (5) Å	1.536 Å	1.571 Å
$C(1)-O(1)$	1.291 (5)	1.304	1.349
$C(1)-O(2)$	1.212 (4)	1.227	1.276
$O(1) \dots O(3)$	2.506 (5)	2.506	2.542
$O(1)-H(1)$	1.026 (7)	1.034	1.132
$O(3)-H(3)$	0.956 (9)	0.986	1.066
$O(3)-H(2)$	0.964 (7)	0.985	1.074
$O(3) \dots H(1)$	1.480 (7)	1.486	1.546

The 'riding' correction is probably a good approximation for the water molecule O-H bond lengths, since this assumes that the center of vibration of the hydrogen atoms is relative to the instantaneous position of the oxygen atom. The 'independent' correction is probably more appropriate for the intermolecular distances. Calculations assuming a rigid body motion of the oxalic acid molecule in  $\alpha$ -DOX (Coppens & Sabine, 1969) predict bond length corrections similar to our riding corrections for  $\alpha$ -POX.

\* 1 f = 1 fermi =  $10^{-15}$  meter.

It is desirable to reduce the bond length corrections by collecting the intensity data at low temperature. Calculations based on the equations below indicate the improvement to be expected. Let the atomic mean square vibration amplitudes  $u^2$  be given by

$$\overline{u^2} = \frac{3h^2T}{4\pi^2mk\theta_M^2} \left\{ \varphi(x) + \frac{x}{4} \right\},$$

where  $m$  is the mass of the atom and  $\theta_M$  the Debye temperature determined by diffraction methods, and

$$\varphi(x) = \frac{1}{x} \int_0^x \frac{\xi d\xi}{\exp(\xi) - 1},$$

where  $x = \theta_M/T$ .

The two possible approximations to the real situation are:

(i) The crystal is best described by an overall Debye temperature.

or,

(ii) A separate Debye temperature should be assigned to each atom.

Calculations for both these conditions have been carried out. On assumption (i), the overall Debye temperature is 141 °K.

The experimentally determined thermal ellipsoid were reduced by  $(u_{77^\circ K}^2)/(u_{298^\circ K}^2)$  and  $(u_{4^\circ K}^2)/(u_{298^\circ K}^2)$  and the thermal corrections to the bond lengths were then recalculated (Table 6). If assumption (i) is correct there is an advantage in reducing the temperature to 4 °K; however, if (ii) is better, it is worthwhile to go to 77 °K but there is no substantial gain in working at 4 °K.

### References

- AHMED, F. R. & CRICKSHANK, D. W. J. (1953). *Acta Cryst.* **6**, 385.  
 BRILL, R., HERMANN, C. & PETERS, C. (1942). *Ann. Phys.* **42**, 357.  
 BUSING, W. R. & LEVY, H. A. (1964). *Acta Cryst.* **17**, 142.

Table 6. Variation in bond length corrections with temperature

$\Delta L$  is the calculated difference between the bond corrections assuming riding and independent thermal motions. (1) is the bond length difference when an overall Debye temperature is assumed, (2) the difference when individual atomic Debye temperatures are used.  $\sigma$  is the e.s.d. in the uncorrected bond length.

	Temperature (°K)	$\Delta L$		
		(1)	(2)	$\sigma$
C(1)—C(1 <sup>1</sup> )	77	0.010 Å	0.015 Å	0.005 Å
	4	0.004	0.012	
C(1)—O(1)	77	0.012	0.017	0.005
	4	0.005	0.014	
C(1)—O(2)	77	0.012	0.017	0.004
	4	0.005	0.013	
O(1)···O(3)	77	0.009	0.011	0.005
	4	0.003	0.011	
O(1)—H(1)	77	0.023	0.027	0.007
	4	0.009	0.026	
O(3)—H(2)	77	0.022	0.027	0.007
	4	0.009	0.019	
O(3)—H(3)	77	0.021	0.026	0.009
	4	0.009	0.018	
O(3)···H(1)	77	0.016	0.019	0.007
	4	0.007	0.013	

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- BUSING, W. R., MARTIN, K. O. & LEVY, H. A. (1962a). ORNL-TM-305. Oak Ridge National Laboratory, Tennessee.  
 BUSING, W. R., MARTIN, K. O. & LEVY, H. A. (1962b). ORNL-TM-306. Oak Ridge National Laboratory, Tennessee.  
 COPPENS, P. & SABINE, T. M. (1969). *Acta Cryst.* **B25**, 2442.  
 DELAPLANE, R. G. & IBERS, J. A. (1969). *Acta Cryst.* **B25**, 2423.  
 GARRETT, B. S. (1954). ORNL-1745. Oak Ridge National Laboratory, Tennessee.  
 MELKONIAN, E. (1949). *Phys. Rev.* **76**, 1750.  
 ROBERTSON, J. M. & WOODWARD, J. (1936). *J. Chem. Soc.* p. 1939.